

Research Article

The Application of Chitosan/*n*TiO₂Nanocomposite in the Elimination of Cu(II) from Aqueous Media: Fixed-Bed Column Adsorption Study and Modelling

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Abstract

The current investigation employed Chitosan/nTiO₂ nanocomposite (CTNC) adsorbent to sequester Cu(II) ions from the aqueous medium by column adsorption. The experimentations were executed at optimum pH 6.5 under variable operating conditions, viz. bed depths (3-7 cm), flow rates (10-30 ml min⁻¹) and Cu(II) concentration (10-30 mg L⁻¹). Seven kinetic models checked experimental records. Thomas model was established to be the best-fit model correlated to a bed height of 5 cm, inner diameter of column 1.5 cm, the influent flow rate of 10 mlmin⁻¹, and the initial Cu(II) concentration of 30 mg L⁻¹. The potential application of multiple linear regression (MLR) and genetic algorithm (GA) techniques to forecast the elimination of Cu(II) are also verified.

Keywords: Chitosan; Nanocomposite; Scale-up; Thomas model; Genetic algorithm

Introduction

Water is a fundamental component of life's presence on the earth. However, nearly all water bodies have become polluted due to ever-increasing population, disorganized urbanization, technological development and voluminous waste production from various anthropogenic sources. It is miserable that 70–80% of the problems in developing countries are related to water pollution [1]. A predominantly severe pollution problem is the contamination of waters by heavy metals due to their portability and toxicity in natural hydrological ecosystems. The



presence of contaminants like Cu(II) at a higher concentration than the tolerance level can give rise to severe, devastating effects on human physiology and other biological systems. Hence, the proper treatment of wastewater is an issue of utmost priority.

Researchers from various fields of science and technology have endeavoured to establish several decontamination processes. However, adsorption is an extensively used technology for sequestration of inorganic and organic pollutants. According to the environmental apprehension, great attention is centred on several works involving chitosan-metal oxide nano-bio composites using a wide range of nano-sized metal-oxides (*n*MOs) to purify the contaminated water by heavy metals.

During the last few decades, the computer processing power has dramatically improved. Therefore, the application of AI has also increased in the same way as depicted by the literature [2,3]. Genetic algorithms and statistical modelling have also become more popular [4]. It is worth venturing into the possibilities of testing the applicability of GA and MLR for the prediction of percentage removal.

This study focuses on the effects of various operating parameters of Cu(II) adsorption by chitosan/nanoTiO₂ nanocomposites (CTNC) in a fixed bed column. The applicability of various kinetic models is studied to explain the breakthrough curve. The application of statistical and genetic algorithm modelling on the data collected from the experiment has also been successfully applied to calculate the percentage removal of Cu(II)

Experimental

Materials

Analytical laboratory grade reagents, namely chitosan powder, acetic acid, 25% glutaraldehyde solution, nano titanium(IV) oxide powder ethanol, copper sulphate pentahydrate (CuSO₄, 5H₂O), NaOH pellets, hydrochloric acid from E. Merck India Limited and doubly distilled water were employed throughout all the experiments.

Methods

Preparation of adsorbent (chitosan/*n*TiO₂ nanocomposite)

Based on our earlier study, Chitosan/nTiO₂ nanocomposite (CTNC) adsorbents were prepared with different chitosan:nTiO₂ (W/W) ratios. Amongst those, chitosan:nTiO₂ (W/W)= 1:1 (CTNC1-1) was most promising for Cu(II) elimination in batch mode [5]. Hence, the adsorbent CTNC1-1 is chosen for the fixed-bed column method.

Characterization

SEM analysis, FTIR studies, BET analysis, XRD studies, TGA, and calculation of the point of zero charges (pH_{PZC}) were done previously [4].



Adsorbate solution preparation

The synthetic Cu(II) stock solution dissolved 3.929 g of copper sulphate pentahydrate in 1 L water. The stock solution was diluted to form the desired concentrated solution.

Column adsorption experimentation

Cu(II) adsorption from aqueous media was done within a fixed bed column at an initial metal concentration ranging from 10-30 mg L^{-1} , bed height ranging from 3-7 cm and flow rate ranging from 10-30 ml min⁻¹ using three glass columns 33 cm long and with an inner diameter of 1.5 cm. A stainless-steel sieve plate was provided as base support, and a little glass wool was placed over it. The columns were packed with the requisite amount of adsorbent. The influent Cu(II) solution was allowed to pass through the columns using a peristaltic pump (Model 7535-04, Cole-Parmer, USA) in down-flow mode at optimum pH 6.5 [5] and room temperature. The resultant Cu(II) solution was quantified using AAS (AA 240 VARIAN, Australia Varian Spectra AA 55, USA) by the standard procedure [6] at set intervals.

The percentage removal efficiency was calculated using Eqs. (1-3) [7,8].

%
$$removal = \frac{q_{total}}{m_{total}} \times 100$$
 (1)

Where

$$q_{total} = QC_0 \int_0^{t_{total}} \left(1 - \frac{C_t}{C_0}\right) dt$$
(2)

And

$$m_{total} = QC_0 t_{total} \tag{3}$$

The experimental uptake capacity $q_{e(exp)}$ is calculated by Eq. (4) [9]

$$q_{e(\exp)} = \frac{q_{total}}{m_d} \tag{4}$$

MLR analysis

For the equation related to multiple linear regression, all the independent variables as chosen for this study are bed height (Z), column diameter (D_c) , flow rate (Q), time (t), influent concentration (C_o) and residual concentration (C_t), and the dependent variable was removal percentage of Cu(II), i.e., $PR_{Col-TiO_2-Cu(II)}$

Genetic algorithm

The applicability of GA depends on the processing time associated with the training. The training process in GA is associated with computerized programming that involves several values (inputs and outputs) relating to some data collected from the experimentation



concerned with a problem. Training time is reduced with the fast-processing power of a microprocessor, RAM, etc.

The data used in the case of MLR has been replicated three times with successive rows and columns to have 3 samples *viz*. Cu(II)-R₁, Cu(II)-R₂ and Cu(II)-R₃. The inputs are the MLR analysis parameters and are presented in Table 3. In the next step, randomization for the 3 sets is carried out (independent of each other) to omit all types of random error that can arise during the training. This step is essential for generalization. Then, the portion of the data used for final prediction (i.e., 10% of the overall data about each set) was segregated and kept aside for these 3 samples, respectively. Following the same process, cross-validation (i.e., 20% of the data about each set) is segregated and kept separate for these 3 samples. Finally, 70% of the overall data about each set is kept for training. The optimization of inputs is performed using a well-known training algorithm (Levenberg-Marquardt), as evidenced by the literature survey [4,5].

Results and discussion

Characterization of adsorbents

The details of SEM analysis, FTIR studies and BET analysis, XRD studies, TGA, point of zero charge (pH_{PZC}) were described in our earlier work [5].

Effects of process parameters

Influence of bed depth

The adsorption experiments were carried out at various bed heights, 3 cm, 5 cm and 7 cm, (Figure 1) with constant metal ion concentration, 10 mg L^{-1} and constant flow rate, 10 ml min⁻¹. Breakthrough and exhaustion time were raised with bed height, signifying improved Cu(II) removal due to greater accessibility of adsorptive sites and higher bed residence time at greater bed depth [8].





Figure 1: Effect of variation of bed depth.

Impact of influent flow rate

The adsorption experiments were carried out at various influent flow rates, 10-30 ml min⁻¹, (Figure 2) at fixed bed height, 3 cm and influent Cu(II) concentration, 10 mg L⁻¹. Breakthrough and exhaustion time reduced with flow rate, signifying less Cu(II) removal due to less contact time and reduced film diffusion resistivity of the adsorbate on the adsorbent at increased flow rates [7].





Figure 2: Effect of variation of influent flow rate.

Influence of influent metal concentration

The experimental observations were recorded at various influent dye concentrations (10-30 mg L^{-1}) (Figure 3) at constant bed height (5 cm) and constant flow rate (10 ml min⁻¹). Breakthrough time, as well as exhaustion time, are reduced with Cu(II) concentration, signifying less Cu(II) removal due to a faster rate of diffusional mass transfer and faster saturation rate of binding centres at higher Cu(II) concentration [7,8].





Figure 3: Effect of variation of initial Cu(II) concentration.

Kinetic Study

Seven kinetic models were employed to evaluate the experimental records. The calculated values of kinetic parameters with correlation coefficients values, the kinetic equations and their interpretations are detailed in Table 1.

Higher R^2 value (i.e., close to 1) indicates the excellent agreement of calculated adsorption capacities obtained from the model equation with experimental data. Hence, from Table, the adsorption process might be best explained by the Thomas model, which was employed for scale-up design.

Initial	Cu(II)	10	10	10	20	30	10	10
concentratio	n, C_0							
$mg L^{-1}$								
Influent flow	w rate,	10	10	10	10	10	20	30

 Table 1: Kinetic models of column study.



Q									
Red height 7		3	5	7		5	5	3	3
cm		5	5	/		5	5	5	5
Experimental		8 266	6 653	6 811		9 2 2 4	11 093	10.2	6718
Adsorption		0.200	0.025	0.011		2.221	11.075	10.2	0.710
capacity. <i>q</i>									
$mq q^{-1}$									
Bohart-Adam	s mod	el (Bol	hart & Ada	$\frac{1}{1920}$) [101			
Mathematical	l equat	tion		amo, 1720 _.	(Comments			
$\ln\left(\frac{C_{t}}{C_{0}}\right) = K_{BA}C_{0}t - K_{BA}N_{0_{BA}}\left(\frac{Z}{U_{0}}\right)$ $K_{BA} = 0.00068 = 0.00066 = 0.00050$			Based on the surface reaction theory, this model assumes that the equilibrium is not attended in a continuous adsorption process, and the adsorption rate is proportional to the adsorption capacity.The rate constant K_{BA} decreased with bed height and influent concentration but increased with flow rate. The adsorption capacity of the bed $N_{0_{BA}}$ decreased with bed depth but increased with influent concentration.0.000410.000260.000710.00116						
$N_{0_{BA}}$	6.326	5	6.127	5.80		8.960	11.461	8.752	6.592
R^2	0.811	52	0.84359	0.82767		0.82749	0.91295	0.89462	0.89375
Thomas mode	el (Tho	mas, 1	944) [11]			•			
Mathematical	l equat	tion			Comments				
$\ln\left(\frac{C_0}{C_t} - 1\right) = \frac{K_{Th}q_{Th}m}{Q} - K_{Th}C_0t$				This model assumes the Langmuir kinetics for adsorption–desorption and the rate of the driving force is the second-order reversible reaction kinetics with no axial dispersion in the column. The rate constant K_{Th} decreased with bed depth and influent concentration but increased with flow rate. Maximum adsorption capacity a_{-} increased with influent concentration					
K _{Th}	1.107	7	1.048	0.816	-	0.6975	0.458	1.38	3.103
mlmg ⁻¹ min ⁻¹									
q_{Th}	8.505	5	6.747	6.898		9.358	11.261	10.220	6.482



\mathbb{R}^2	0.9474	0.9521	0.9477	0.9534	0.9745	0.9588	0.9668
Wolborska m	odel (Wolbo	orska, 1989)	[12]				
Mathematical	equation	,		Comments			
$\ln\left(\frac{C_t}{C_0}\right) = \frac{\beta_W C_0 t}{N_{0_W}} - \frac{\beta_W Z}{U_0}$				This mode distribution concentratio curve.	describe in the fiz n region	s the convert r the convert r the bed at of the brown r	the low eakthrough
					coefficient	ρ_{W} values	Increased
				with an inc with influen adsorption c	rease in flo t concentration capacity of	fow rate but ion and bed N_{0_w} the bed	decreased depth. The increased
				with influen bed depth.	t concentrat	ion but decr	eased with
β_W min ⁻¹	4.283	4.056	2.888	3.665	2.930	6.205	7.674
$\frac{N_{0_W}}{\mathrm{gL}^{-1}}$	6.326	6.127	5.780	8.960	11.461	8.752	6.592
R^2	0.8115	0.8436	0.8277	0.8275	0.9130	0.8946	0.8938
Yoon-Nelson	model (You	on & Nelson	, 1984) [1.	3]			
Mathematical	equation			Comments			
$\ln\left[\frac{C_t}{\left(C_0 - C_t\right)}\right] = k_{YN}t - \tau_{YN}k_{YN}$				This model assumes that the probability rate of adsorption decreases for each adsorbate is proportional to the probability of its adsorption and breakthrough on the adsorbent surface.			
				The half-life of adsorbate (τ_{YN}) decreased			
				with flow rate and influent concentration but increased with bed height. The rate constant			
				$K_{\rm m}$ increased with flow rate but decreased			
				with had depth			
K_{YN} min ⁻¹	0.01107	0.01048	0.00816	0.01395	0.01374	0.0138	0.03103
$ au_{YN}$	337.305	391.204	514.158	271.299	217.633	217.633	85.6980
min	0.04-4	0.0701	0.04==	0.0704	0.0747	0.0700	0.0.440
K ²	0.9474	0.9521	0.9477	0.9534	0.9745	0.9588	0.9668
Yan <i>et al</i> . moo	del (Yan et a	al., 2001) [1	4]	<u>a</u>			
Mathematical	equation			Comments			
$\ln\left[\frac{C_t}{\left(C_0 - C_t\right)}\right] = \frac{K_Y C_0}{Q} \ln\left(\frac{Q^2}{K_Y q_Y m}\right) + \frac{K_Y C_0}{Q} \ln t$			It is an em drawback of the prediction	pirical equation the Thoma	ntion to ove s model, esp nt concentra	becially for tion nearly	



			at the time zero.						
			The rate constant K_{γ} increased with increasing						
			bed depth and flow rate but decreased with						
				influent con	centration.	Maximum	adsorption		
				capacity q_y i	ncreased wi	th increasin	g flow rate		
				and influent	concentrati	on but decr	eased with		
				bed depth.					
K _y	2.064	2.099	2.566	1.061	0.553	3.323	6.182		
mlmg ⁻¹ min ⁻¹									
	0.0420	0.0232	0.0115	0.0697	0.1651	0.1821	0.5526		
moo ⁻¹									
R^2	0.9393	0.9062	0.9321	0.9153	0.8729	0.8514	0.8328		
Modified dose	e-response i	model (Yan	et al., 200	01) [14]	0.0725	0.0011	0.0220		
Mathematical	equation	X	,	Comments					
				It is an	empirical	model dev	reloned to		
$\ln \left \frac{C_t}{C_t} \right $	$=a_{m,ln}\ln(C_{ln})$	$Q(t) - a \ln(a)$	(m,m)	minimize th	e error pres	sented by the	ne Thomas		
$\left\lfloor \left(C_0 - C_t \right) \right\rfloor$	mar ()	<i>(</i> ∠)	mar)	model at the	e lower and	higher por	tion of the		
				breakthrough	n curve.				
				Maximum adsorption capacity a , increased					
				with influent concentration The model					
				narameter <i>d</i>	increased	with bed d	enth		
	2.064	2,000	2566	2.122			2.061		
a_{mdr}	2.004	2.099	2.300	2.122	1.000	1.002	2.001		
$q_{\scriptscriptstyle mdr}$	7333.50	6104.88	6117.84	8046.42	9768.73	8406.53	5024.14		
mgg ⁻¹									
R ²	0.9393	0.9062	0.9321	0.9153	0.8729	0.8514	0.8328		
Bed depth ser	vice time n	nodel (Chen	et al., 201	3) [15]					
Mathematical	lequation			Comments					
$N_{0_{bdst}}Z$	1 $l_{\rm ln} \left(C_{\rm o} \right)$) 1		This model is used to predict the bed capacity					
$l = \frac{1}{C_0 U_0} - \frac{1}{K}$	$\overline{C_{h,det}C_0}^{\text{III}} \left(\overline{C_{t}} \right)$			using different breakthrough values. The					
0 0	basi 0 C i			BDST model parameters can help scale up the					
				process for other flow rates without further					
				experimental runs. The graph of t vs. Z does					
			not pass through the origin, indicating that the						
			adsorption process is complex and involves						
			more than of	ie rate-limit	ing step.				
			The values of $N_{0_{bdst}}$ and K_{bdst} increased with						
						C_{t}			
				increasing ($\frac{1}{t}$ values				
				increasing $\frac{C}{C}$	$\frac{\sum_{t}}{\sum_{0}}$ values.				
<i>C</i> ,	No		K	increasing $\frac{C}{C}$	$rac{C_t}{C_0}$ values.				



0.1	1.2592	-0.00659	0.9505
0.5	2.7621	0	0.9975
0.9	3.4143	0.000658	0.8937

Scale-up design

The consideration of scale-up designing was important for lab-to-land implementation. Based on the best-fitted kinetic model, a scale-up design was developed for the fixed-bed column study.

Thomas model was established to be the best-fit model corresponding to 5 cm bed height, 10 ml min⁻¹influent flow rate, and the influent Cu(II) concentration 30 mgL^{-1} .

Table 2: Scale-up	designfor adsorption	of Cu(II) by CTNC1-1	in fixed bed column.
I ubic 2 . Deule up	designioi description		

W m ³	t_w min	Cw mg L ⁻¹	Qd L min ⁻¹	D m	M _{ad} kg/day	Hc m	H m
10	480	30	20.83	0.68	3.22	0.4	0.401
20	600	30	33.33	0.87	5.15	0.5	0.501

Eqs. (5-8) [7,8] were involved in estimating parameters presented in Table 2 for scale-up design in the column adsorption mode.

$$Q_d = \frac{\pi D^2 U_0}{4} \tag{5}$$

Where,

$$D = \sqrt{\frac{4W}{\pi t_W U_0}} \tag{6}$$

$$M_{ad} = \frac{Q_d C_w}{q_{ad}} \int_0^{t_R} \left(1 - \frac{C_t}{C_w}\right) dt$$
(7)

Here t_R is the bed regeneration time corresponding to $C_t \leq C_d$

$$H = H_c + \frac{4M_{ad}}{\pi D^2 \rho_{ad}} \tag{8}$$

Regeneration study

According to the previous desorption study [5], the regenerated adsorbent was re-utilized in the column. The regeneration efficiency was found to be 76.38 % from Eqs. (9-10).



$$\varepsilon = \frac{q_R}{q_{total}} \times 100\%$$
$$q_R = Q \int_0^{t_{RS}} (C_0 - C_t) dt$$
(10)

MLR study

The data accumulated from the experiment to predict $PR_{Col-TiO_2-Cu(II)}$ using MLR is stated in Table 3.

Parameter	Range
Bed height, $Z(m)$	0.03-0.07
Column diameter, $D_c(m)$	0.015
Flow rate, Q (ml/min)	10-30
Time, t (min)	0-840
Influent Conc., C_O (mg/L)	10-30
Residual Conc., C_t (mg/L)	0-30
Percentage removal, $PR_{Col-TiO_2-Cu(II)}$ (%)	0-100

Table 3: Description	of data	for MPR.
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The data from Table 3 yielded the following first-degree polynomial equation for measuring the removal efficiency of Cu(II) by CTNC1-1.

$$PR_{Col-TiO_2-Cu(II)} = 1.061574 - 0.258007 \times Q + 0.162926 \times Z -0.87901 \times t + 0.046228 \times C_o - 0.840078 \times C_t$$
(11)

The variance, mean squared error and correlation coefficient achieved from Eq. (11) are 0.056125, 0.00315 and 0.9742 respectively. In this case, the *t*-value is 1.9703 (231 degree of freedom, within the 95% confidence range). Figure 4 depicts the comparison plot using MLR.

(9)





Figure 4: MLR comparison plot.

Data analysis with Genetic algorithm

The processes of training, as well as the cross-validation, are simultaneous. However, it was not allowed for perpetuity, but a limitation of 500 epochs is set for the overall process. At most, 100 iterations are allotted to improve MSE (mean squared error) associated with cross-validation. During the iterative process, training is halted if no improvement is observed. The least amount of error values (cross-validation) observed during the training process is recorded, and the network with these values of weights for this iteration is considered an optimized network.

Then the GA process is observed to find the generation for which the least value of generation error is achieved. Slight modification concerning the chromosomes is done for this process while maintaining the probability value associated with a mutation at 0.1. The crossover probability value is kept at 0.9. Ananalogous type of processing had been done by researchers, as evident from the literature review [16,17]. That generation was considered optimal once the generation error achieved a value around 10^{-6} – 10^{-7} . Table 4 depicts the generation errors and the subsequent results related to the GA analysis. Thus, the observations of Table 4 and Figure 5 establish that the R-value of unity is achieved for these samples. The observations validate the efficient forecast of the percentage removal of the adsorbate.



Randomization No.	Minimum Generation error	AARE	SD (σ)	MSE	CCC (R)
$Cu(II)R_1$	4.0447×10 ⁻⁸	0.00029	0.0004	0.00024	1
Cu(II)R ₂	1.0103×10 ⁻⁷	0.00028	0.00025	0.00038	1
Cu(II)R ₃	3.9035×10 ⁻⁷	0.00169	0.00389	0.00132	1

Table 4: Performance of the optimized network using GA.





Conclusion

The potency of CTNC1-1 for eliminating Cu(II) from aqueous mediaby fixed-bed column technique at different operating situations was evident from this work. The outcomes might be abbreviated like this:



- The bed depth of CTNC1-1 influenced the removal of Cu(II) within the column, influent flow rate and metal ion concentration.
- The removal was raised with bed depth and reduced with influent flow rate and Cu(II) concentration.
- The Thomas model brilliantly described the kinetic process with a good correlation.
- The usefulness of the CTNC1-1 adsorbent can be recommended from the scale-up design of the adsorption column.
- The MLR, and GA, also predicted the percentage removal with acceptable statistical accuracy.

Nomenclature

a_{mdr}	Modified dose-response kinetic model parameter
C_0	Influent Cu(II) concentration (mg L^{-1})
C_d	Cu(II) discharge limit for inland surface water (mg L ⁻¹)
C_t	Effluent Cu(II) concentration at time t (mg L^{-1})
C_w	Cu(II) concentration in wastewater (mgL ⁻¹)
D	Diameter of the adsorption column (m)
H	Total bed height in the column (m)
H_c	Additional height for accessories (m) $U_{1} = \frac{1}{2} = \frac{1}{2}$
K _{BA}	Kinetic constant in Bohart-Adams model (L mg ⁻¹ min ⁻¹)
K _{bdst}	Kinetic constant in Bed depth service time model (L $mg^{-1} min^{-1}$)
K_{YN}	Kinetic constant in Yoon-Nelson kinetic model (L $mg^{-1} min^{-1}$)
K _{Th}	Kinetic constant in Thomas model (ml mg $^{-1}$ min $^{-1}$)
K_{Y}	Kinetic constant in Yan et al. model (ml $mg^{-1} min^{-1}$)
M_{ad}	Designed adsorbent quantity (kg)
m_d	Mass of dry adsorbent in column (g)
m_{total}	Mass of the adsorbate added to the column (g)
$N_{0_{\scriptscriptstyle B\!A}}$	Bohart-Adams model adsorption capacity of bed (mg L^{-1})
N_{0_W}	Wolborska model adsorption capacity of bed (mg L^{-1})
$N_{0_{bdst}}$	Bed depth service time model adsorption capacity (gL ⁻¹)
Q	Volumetric flow rate (ml min ⁻¹)
Q_d	Designed volumetric flow rate (ml min ⁻¹)
$q_{e(\exp)}$	Experimental adsorption capacity (mg g ⁻¹)
$q_{\scriptscriptstyle mdr}$	Modified dose–response model maximum adsorption capacity (mg g^{-1})
q_{R}	Amount of Cu(II) adsorbed after regeneration (mg)
$q_{\scriptscriptstyle Th}$	Thomas model maximum adsorption capacity (mg g ⁻¹)
$q_{\scriptscriptstyle Y}$	Yan et al. model maximum adsorption capacity (mg g^{-1})
q_{total}	Total Cu(II) adsorbed (mg)



t	Time (min)
t_R	Bed regeneration time (min)
t_{RS}	Bed saturation time after regeneration (min)
t_{total}	Total flow time (min)
t_W	Working time (min)
U_0	Superficial velocity (cm min ⁻¹)
V_{eff}	Effluent volume (L)
W	Daily wastewater flow (m ³)
Ζ	Bed depth (cm)

Greek letters

β_W	Kinetic coefficient of external mass transfer in Wolborska model (min ⁻¹)
З	Regeneration efficiency
$ ho_{\scriptscriptstyle ad}$	Density of the adsorbent (kg m^{-3})
$ au_{_{Y\!N}}$	Half life of adsorbate (min)

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